Bedrock: A Framework for Verifying Low-level Programs

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Harvard University SEAS

IBM PL Day '12 – June 28

Type Safety Isn't Always Enough!

```
let getFirst (buf : 'a array) : 'a option :=
  let len = Array.length buf in
  if len = 0 then None
  else Some (Array.get buf (len − 1))
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Why not negative?

Type Safety Isn't Always Enough!

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Why not negative?

Index out of bounds?

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Most informative text!

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Type Safety Isn't Always Enough!

Most informative text! oops!

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let getLast (buf : 'a array) : 'a option :=
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Project Goals

A programming language for systems code that supports

- verification down to the machine code ...

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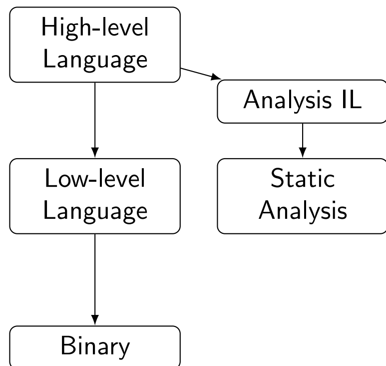
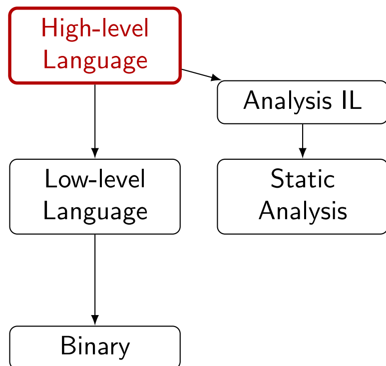
Bedrock

Typical Program Verification



Typical Program Verification



- Focus is on the high-level language!

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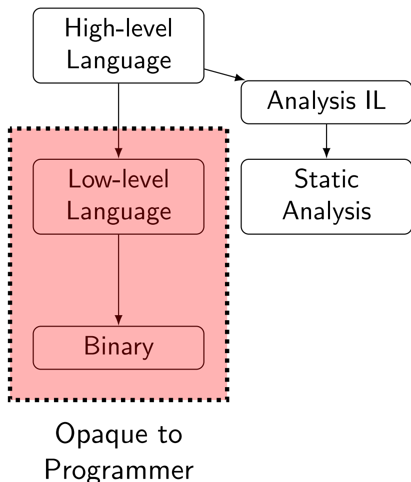

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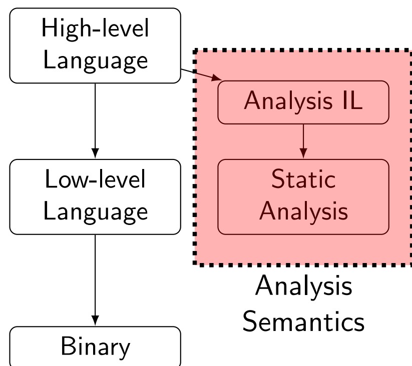

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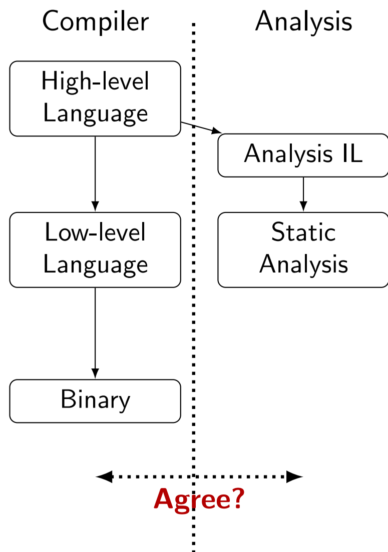
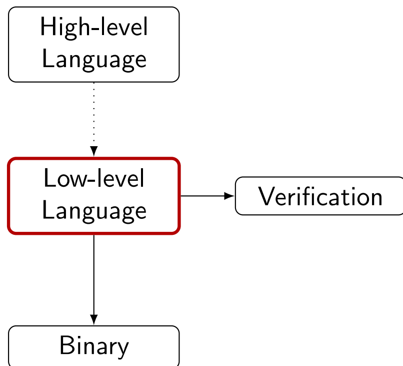


- Focus is on the high-level language!
- Compiler focuses on converting to a binary.
- Need the same semantics.

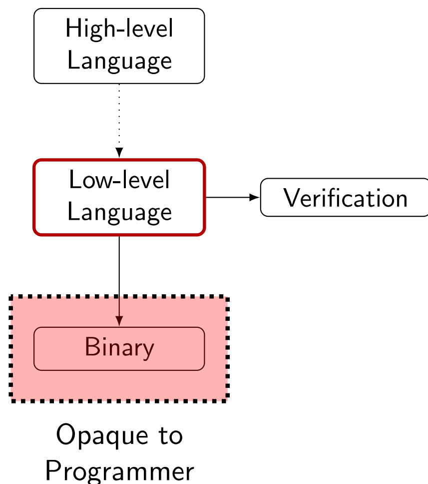
Verification in Bedrock

- Focus is on a low-level language.



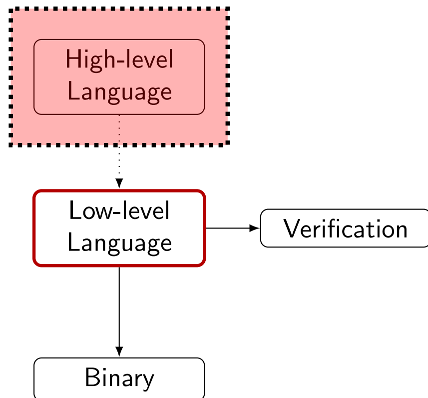
Verification in Bedrock

- Focus is on a low-level language.
- Minimal details hidden by the framework.



Verification in Bedrock

- Focus is on a low-level language.
- Minimal details hidden by the framework.
- Achieve abstraction by parametrization over the semantics.



Outline

1. Programming in Bedrock2
   - A Simple Program
   - Extensible Control
   - Memory
   - Verification with Abstract Data Types
   - Strongest Post-condition of Data Abstractions
2. Making it Automatic
3. Current & Future Directions

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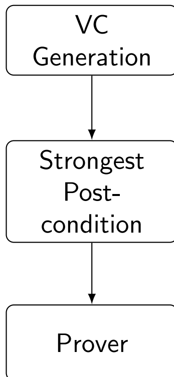
Verifying a Simple Program

A Simple Program

```
{Rp @@ (st' ~> st'.Rv = 0)}
Rv := 0 ;
goto Rp
```

Verifying a Simple Program



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Strongest Post-condition

```
{Rp@@(st' ~> st'.Rv = 0)} st
∧ evalInstrs st [ Rv := 0 ] st'
→ { Rv = 0 } st'
```

VC Generation → Strongest Post-condition → Prover

Verifying a Simple Program

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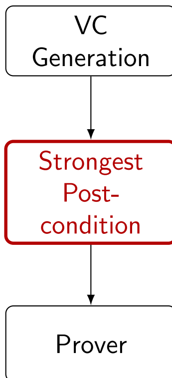

Verifying a Simple Program

A Simple Program

```
{Rp @@ (st' ~> st'.Rv = 0)}
Rv := 0 ;
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Proof Obligation

```
{Rv = 0 ∧
 Rp @@ (st' ~> st'.Rv = 0)} st'
→ { Rv = 0 } st'
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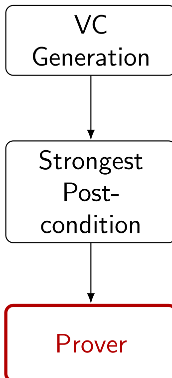

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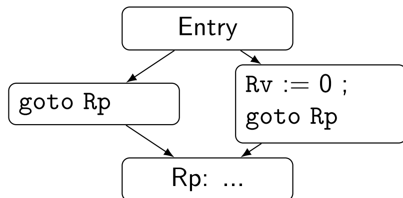
Bedrock2: Extensible Control

Conditional Code

```
{ Entry : ([],  br Rv Eq 0 Tr Fa)
; Tr    : ([],  goto Rp)
; Fa    : ([ Rv := 0],  goto Rp) }
```



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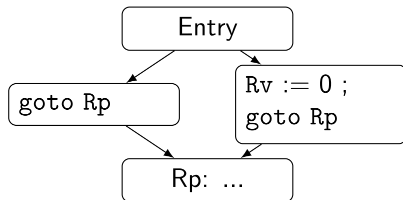

This looks like if!

Bedrock2: Extensible Control

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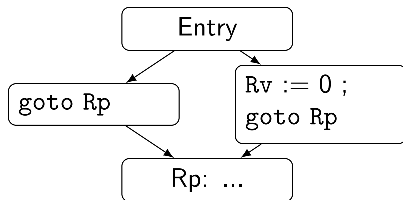

This looks like if!

Abstract it!

Control Abstraction

- Build syntax combinators in the meta-language

If Combinator

```
Definition If (cmp : Cmp) (l : Rhs) (r : Rhs) (tr : Code) (fa : Code) :
    Code := ...
```

Control Abstraction

- Build syntax combinators in the meta-language

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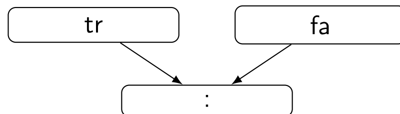

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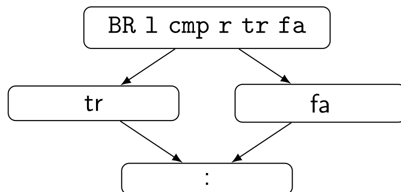

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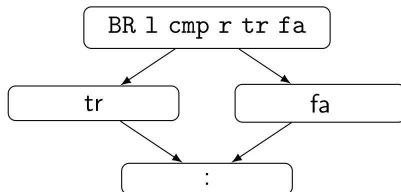

Don't want to reason about this every time

Verified Control Abstraction

- Package the combinator with a proof rule.
- Verify the proof rule once.

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If Combinator Sketch

```
let If cmp l r tr fa := fun P ⇒
  let tr := tr (P ∧ cmp l r = true) in
  let fa := fa (P ∧ cmp l r = false) in
  { Ent : L
  ; Blocks : { L : (BR cmp l r tr.Ent fa.Ent) } ∪ tr.Blocks ∪ fa.Blocks
  ; Post : tr.Post ∨ fa.Post
  ; Safe : safeTest l cmp r ∧ tr.Safe ∧ fa.Safe
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If Combinator Sketch

Precondition

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Add branch fact

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Combine the blocks

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Combine post condition

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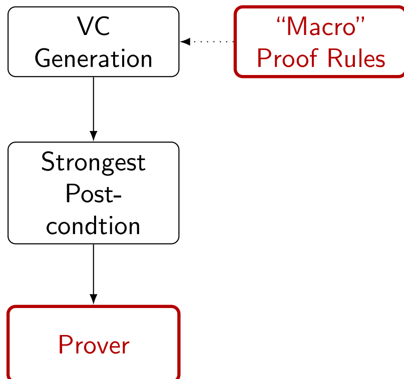
```

Combine safety conditions

Verification with Extended Control

Always-0 with Conditionals

```
{Rp @@ (st' ~> st'.Rv = 0)}
If (Rv = 0) {
  skip
} Else {
  Rv := 0
} ;
goto Rp
```



Verification with Extended Control

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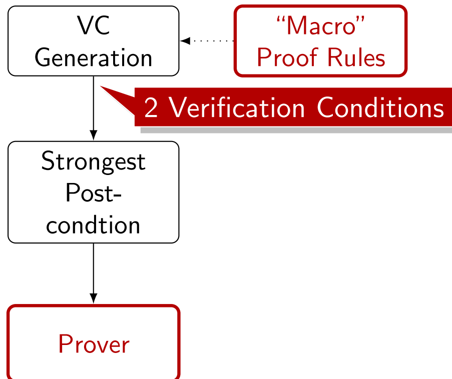
New VC

```
{Rp@@(st' ~> st'.Rv = 0)} st
∧ evalCond st (Rv = 0)
→ { Rv = 0 } st
```



Verification with Extended Control

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Proof Obligation

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{Rp@@(st' ~> st'.Rv = 0)
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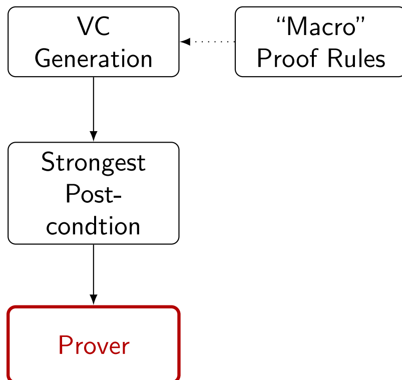

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Verification with Memory

Always-0 with Memory

```
{ ∃ v, ![Rv ↦ v] ∧
  Rp @@ (st' ~> ![Rv ↦ 0] st') }
$[Rv] := 0 ;
goto Rp
```

Verification with Memory

Always-0 with Memory

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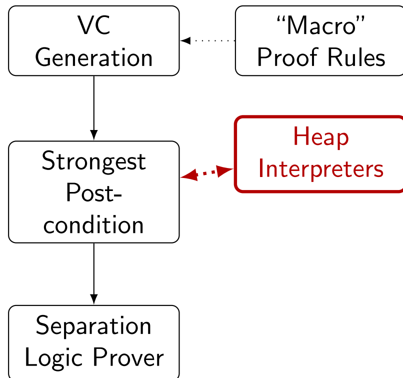

Verification with Memory

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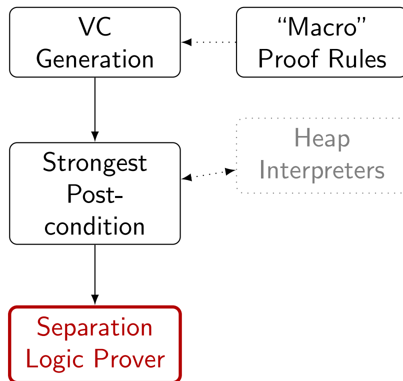

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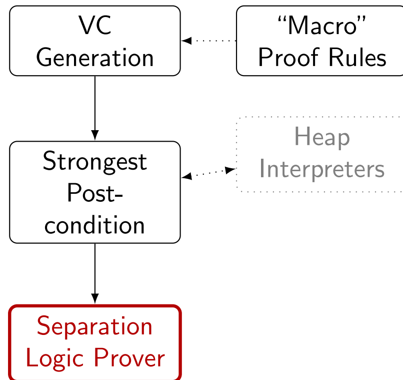
Proof Obligation

```
{ Rp @@ (st' ~> ![Rv ↦ 0] st') st
  ![ Rv ↦ 0] } st
→ { ![Rv ↦ v] } st
```



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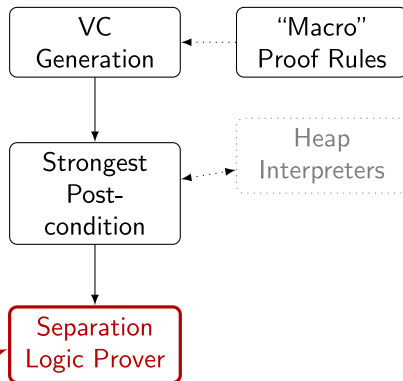
Proof Obligation

```
{ Rp @@ (st' ~> ![Rv ↦ 0] st') st
  ![ Rv ↦ 0] } st
→ { ![ Rv ↦ v] } st
```

```
(True → True) ∧
(Rv ↦ 0) ⇒ (Rv ↦ v)
```



A Simple Separation Logic Prover

- Solve implications by repeated cancellation

A Simple Goal

$$p_2 \mapsto v_2 * p_1 \mapsto v_1 * P \Rightarrow P * p_1 \mapsto v_1 * p_2 \mapsto v_2$$

A Simple Separation Logic Prover

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$$p_2 \mapsto v_2 \quad \Rightarrow \quad p_2 \mapsto v_2$$

A Simple Separation Logic Prover

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A Simple Goal

$$\emptyset \quad \Rightarrow \quad \emptyset$$

- Proves $\emptyset \Rightarrow \emptyset$ by reflexivity.

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Reasoning about Abstract Data Types: Lists

Linked List Head

```
{ ∃ ls, ![llist Rv ls] st ∧
  Rp@@(st'~> ![llist st.Rv ls] st'
  ∧ st'.Rv = hd ls) }
If (Rv = 0) { skip }
Else { Rv = $[Rv] } ;
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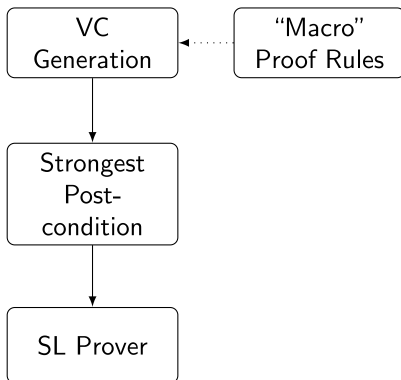


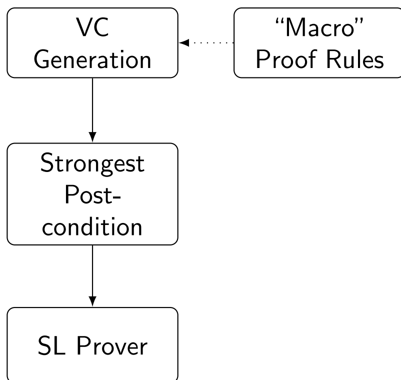
Reasoning about Abstract Data Types: Lists

Linked List Head

```
{ ∃ ls, ![llist Rv ls] st ∧
  Rp@@(st'~> ![llist st.Rv ls] st'
  ∧ st'.Rv = hd ls) }
If (Rv = 0) { skip }
Else { Rv = $[Rv] } ;
goto Rp
```

Symbolic Evaluation

```
{∃ ls, ![llist Rv ls] ∧ Rv ≠ 0} st
∧ evalInstrs st [Rv := $[Rv]] st'
→ {∃ ls, ![llist st.Rv ls]
    ∧ st'.Rv = hd ls} st'
```



Reasoning about Abstract Data Types: Lists

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Symbolic Evaluation

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{∃ ls, ![llist Rv ls] ∧ Rv ≠ 0} st
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→ {∃ ls, ![llist st.Rv ls]
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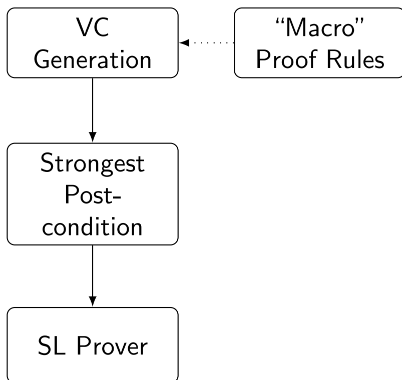
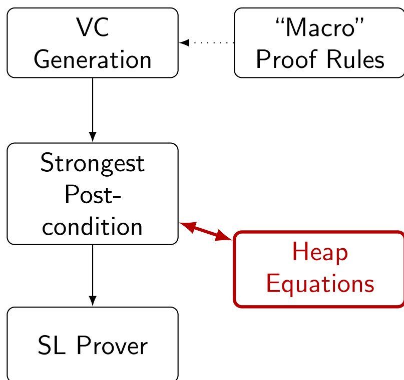
```

Stuck!



Reasoning about Abstract Data Types: Lists



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Symbolic Evaluation

```
{∃ ls, ![llist Rv ls] ∧ Rv ≠ 0} st
∧ evalInstrs st [Rv := $[Rv]] st'
→ {∃ ls, ![llist st.Rv ls]
    ∧ st'.Rv = hd ls} st'
```

```
∀ p ls, p <> 0 →
llist p ls ⇒ ∃ v p' ls', p ↦ v *
  p+4 ↦ p' * llist p' ls' *
  ls = v :: ls'
```

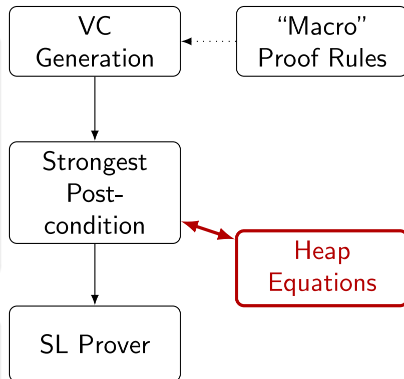
Reasoning about Abstract Data Types: Lists

Linked List Head

```
{ ∃ ls, ![llist Rv ls] st ∧
  Rp@@(st'~> ![llist st.Rv ls] st'
  ∧ st'.Rv = hd ls) }
If (Rv = 0) { skip }
Else { Rv = $[Rv] } ;
goto Rp
```

Symbolic Evaluation

{∃ p' v ls', ls = v :: ls' ∧ Rv≠0 ∧
![Rv ↦ v ∗ Rv + 4 ↦ p' ∗ llist p' ls']} st
∧ evalInstrs st [Rv := $[Rv]] st'
→ {∃ ls, ![llist st.Rv ls]
  ∧ st'.Rv = hd ls} st'



∀ p ls, p ≠ 0 →
llist p ls ⇒ ∃ v p' ls', p ↦ v ∗
  p+4 ↦ p' ∗ llist p' ls'

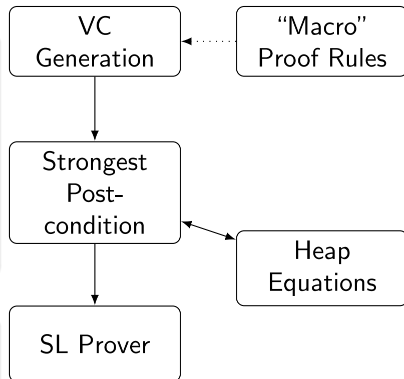
Reasoning about Abstract Data Types: Lists

Linked List Head

```
{ ∃ ls, ![llist Rv ls] st ∧
  Rp@@(st'~> ![llist st.Rv ls] st'
  ∧ st'.Rv = hd ls) }
If (Rv = 0) { skip }
Else { Rv = $[Rv] } ;
goto Rp
```

Proof Obligation

```
{∃ ls p' v ls', ls=v::ls' ∧ Rv=v ∧
![ Rv ↦ v * Rv+4 ↦ p' *
  llist p' ls']} st'
→ {∃ ls p' v ls', Rv = hd ls ∧
![ llist st.Rv ls]} st'
```



Reasoning about Abstract Data Types: Lists

Linked List Head

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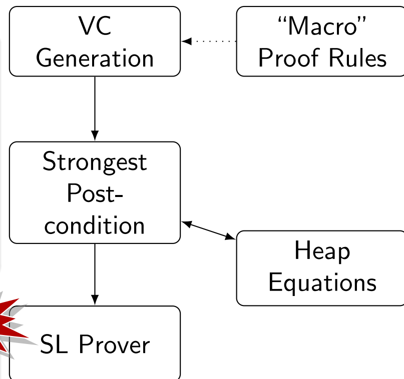
{∃ ls p' v ls', ls=v::ls' ∧ Rv=v ∧
![ Rv ↦ v ∗ Rv+4 ↦ p' ∗
  llist p' ls']} st'
→ {∃ ls p' v ls', Rv = hd ls ∧
![ llist st.Rv ls]} st'
```



Reasoning about Abstract Data Types: Lists

Linked List Head

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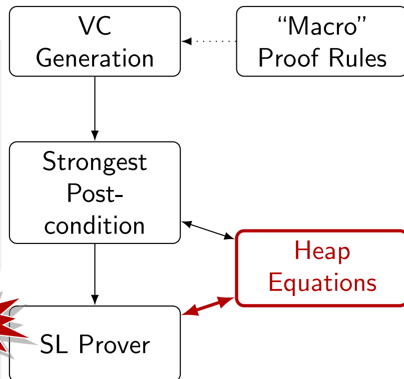
Proof Obligation

```
{∃ ls p' v ls', ls=v::ls' ∧ Rv=v ∧
![ Rv ↦ v * Rv+4 ↦ p' *
  llist p' ls']} st'
→ {∃ ls p' v ls', Rv = hd ls ∧
![ llist st.Rv ls]} st'
```




```
∀ p ls, p ≠ 0 →
 ∃ v p' ls', p ↦ v * p+4 ↦ p' *
  llist p' ls' ⇒ llist p ls
```

Reasoning about Abstract Data Types: Lists

Linked List Head

```
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  Rp@@(st'~> ![llist st.Rv ls] st'
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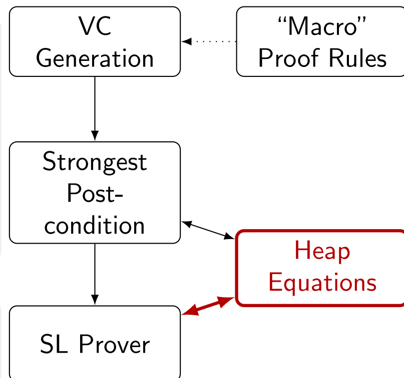
If (Rv = 0) { skip }
Else { Rv = $[Rv] } ;
goto Rp
```

Proof Obligation

```
{∃ ls p' v ls', ls=v::ls' ∧ Rv=v ∧
![ Rv ↦ v * Rv+4 ↦ p' *
  llist p' ls']} st' →
{∃ ls p' v ls', Rv = hd ls ∧
     ls = v :: ls' ∧
![ Rv ↦ v * Rv + 4 ↦ p' * s']} st'
```




```
∀ p ls, p ≠ 0 →
 ∃ v p' ls', p ↦ v * p+4 ↦ p' *
  llist p' ls' ⇒ llist p ls
```

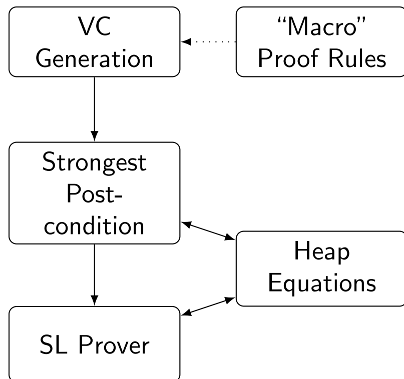
Outline

1. Programming in Bedrock2
   - A Simple Program
   - Extensible Control
   - Memory
   - Verification with Abstract Data Types
   - Strongest Post-condition of Data Abstractions
2. Making it Automatic
3. Current & Future Directions

Strongest Post-condition and Data Abstraction

Read from Array

```
{ ![ Array Rv 1024 0s] st ∧
  Rp @@ ...}
Sp := Rv[100] ;
Rv[100] := Sp ;
goto Rp
```



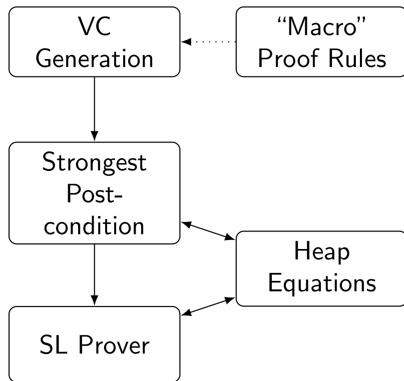
Strongest Post-condition and Data Abstraction

Read from Array

```
{ ![ Array Rv 1024 0s] st ∧
  Rp @@ ...}
Sp := Rv[100] ;
Rv[100] := Sp ;
goto Rp
```

Strongest Post-condition

```
{ ![ Array Rv 1024 0s] } st
∧ evalInstrs st [Sp := Rv[100]; ...]  st'
→ ...
```



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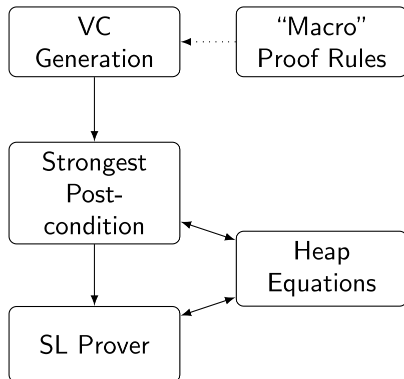
Strongest Post-condition

```
{ ![ Array Rv 1024 0s] } st
∧ evalInstrs st [Sp := Rv[100]; ...]  st'
→ ...
```

Stuck!



Strongest Post-condition and Data Abstraction

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{ ![ Array Rv 1024 0s] st ∧
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Sp := Rv[100] ;
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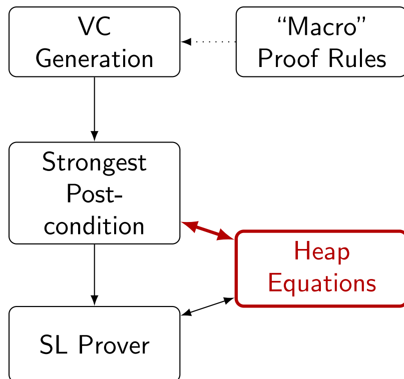
goto Rp
```

Strongest Post-condition

```
{ ![ Array Rv 1024 0s] } st
∧ evalInstrs st [Sp := Rv[100]; ...]  st'
→ ...
```

Bad!



Strongest Post-condition and Data Abstraction

Read from Array

```
{ ![ Array Rv 1024 0s] st ∧
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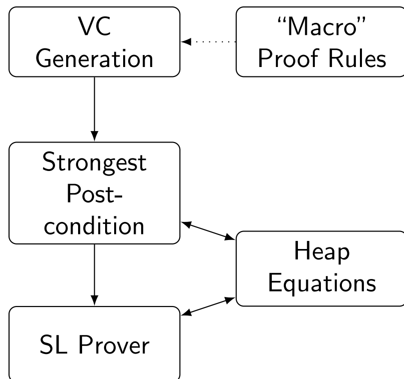
Strongest Post-condition

```
{ ![ Array Rv 1024 0s] } st
∧ evalInstrs st [Sp := Rv[100]; ...]  st'
→ ...
```

Stuck!



Strongest Post-condition and Data Abstraction

Read from Array

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Sp := Rv[100] ;
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Strongest Post-condition

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{ ![ Array Rv 1024 0s] } st
∧ evalInstrs st [Sp := Rv[100]; ...]  st'
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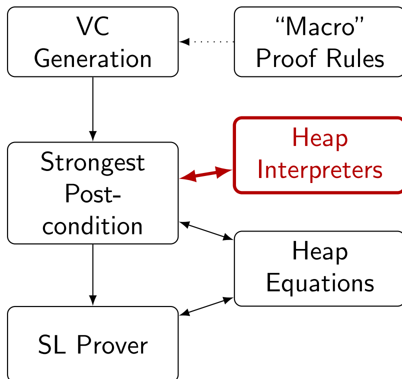

Strongest Post-condition and Data Abstraction

Read from Array

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Sp := Rv[100] ;
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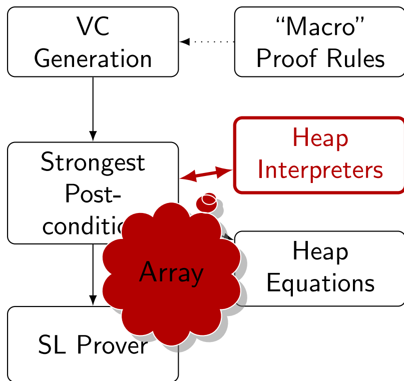
```

Strongest Post-condition

```
{ ![ Array Rv 1024 0s] } st
∧ evalInstrs st [Sp := Rv[100]; ...]  st'
→ ...
```

Stuck!



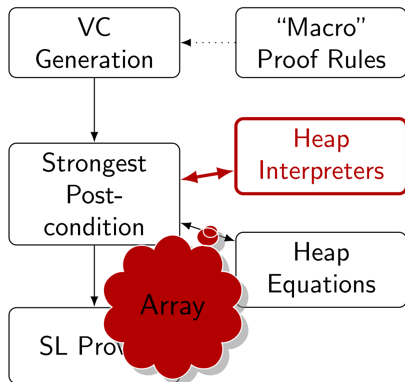
Strongest Post-condition and Data Abstraction

Read from Array

```
{ ![ Array Rv 1024 0s] st ∧
  Rp @@ ...}
Sp := Rv[100] ;
Rv[100] := Sp ;
goto Rp
```

Strongest Post-condition

```
{ ![ Array Rv 1024 0s]
  ∧ Sp = get 0s 100 } st
∧ evalInstrs st [Rv[100] := Sp] st'
→ ...
```



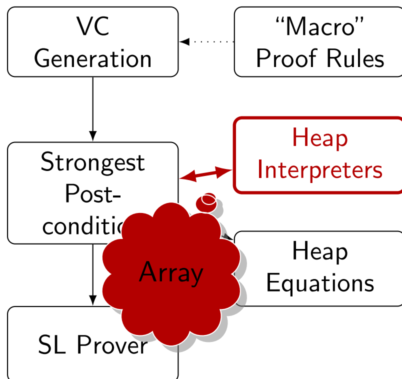
Strongest Post-condition and Data Abstraction

Read from Array

```
{ ![ Array Rv 1024 0s] st ∧
  Rp @@ ...}
Sp := Rv[100] ;
Rv[100] := Sp ;
goto Rp
```

Strongest Post-condition

```
{ ![ Array Rv 1024 (update 100 Sp 0s)]
  ∧ Sp = get 0s 100 } st'
→ ...
```



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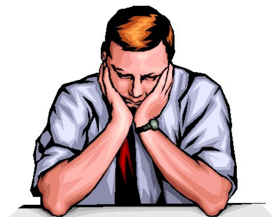
Verification with Computational Proofs



- Constructing proofs can take a long time...
  - Verification needs to be fast.

"Traditional" Proofs: `Even 2048`

Definition of Even

$$\frac{}{\text{Even } 0}\ \text{Even_0}$$

$$\frac{\text{Even } n}{\text{Even } n+2}\ \text{Even_SS}$$

An Easy Proof Script

```
Theorem Even_2048 : Even 2048.
  repeat constructor.
Qed.
```

7s

7s

A **Huge** Proof

$$\cfrac{\cfrac{\cfrac{\cfrac{}{\text{Even } 0}\ \text{Even_0}}{\ldots(1022 \text{ applications})}\ \text{Even_SS}}{\text{Even } 2046}\ \text{Even_SS}}{\text{Even } 2048}\ \text{Even_SS}$$

Proofs by Computational Reflection

Definition of Even

$$\frac{}{\text{Even } 0}\ \text{Even_0}$$

$$\frac{\text{Even } n}{\text{Even } n+2}\ \text{Even_SS}$$

A Prover

```
Fixpoint is_even n : bool :=
  match n with
    | 0 ⇒ true
    | 1 ⇒ false
    | S (S n) ⇒ is_even n
  end.
Theorem is_even_Even : ∀ n,
  is_even n = true → Even n.
Qed.
```

A Good Proof

$$\dfrac{\dfrac{\dfrac{}{\text{true} = \text{true}}\ \text{Reflexivity}}{\text{is_even } 2048 = \text{true}}\ [\text{computation}]}{\text{Even } 2048}\ \text{is_even_Even}$$

Proofs by Computational Reflection

Definition of Even

$$\frac{}{\text{Even } 0}\ \text{Even_0}$$

$$\frac{\text{Even } n}{\text{Even } n+2}\ \text{Even_SS}$$

Total Proof: 0s

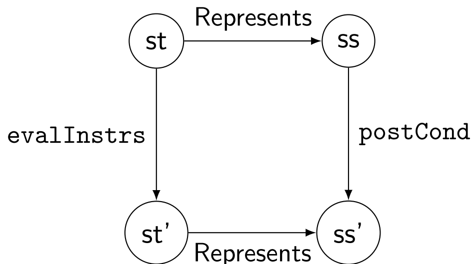
A Prover

```
Fixpoint is_even n : bool :=
  match n with
    | 0 ⇒ true
    | 1 ⇒ false
    | S (S n) ⇒ is_even n
  end.
Theorem is_even_Even : ∀ n,
  is_even n = true → Even n.
Qed.
```

A Good Proof

$$\cfrac{\cfrac{\cfrac{}{\text{true} = \text{true}}\ \text{Reflexivity}}{\text{is_even } 2048 = \text{true}}\ [\text{computation}]}{\text{Even } 2048}\ \text{is_even_Even}$$

Applying Computational Reflection



Reflective Theorem

```
Theorem symEval_sound : ∀ instrs ss ss' st,
  Represents ss st →
  evalInstrs st instrs st' →
  postCond ss instrs = Some ss' →
  Represents ss' st'.
```

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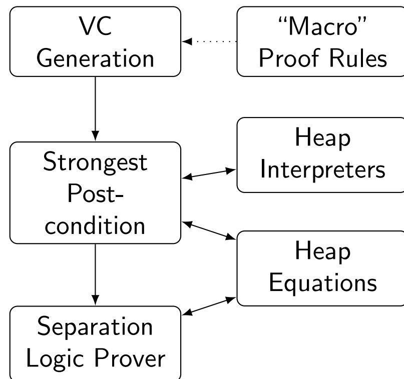
Future Directions

- Extend to other core languages
  - x86, LLVM
- Concurrency
- Low-level interaction
  - Virtual memory
  - Devices
- Optimization

Overview: Bedrock2

- Define higher-level syntax on low-level syntax
- VC generation and symbolic evaluation
- Avoid baking in features
  - Extensible heap interpreters
  - Extensible heap equations
- Separation logic prover



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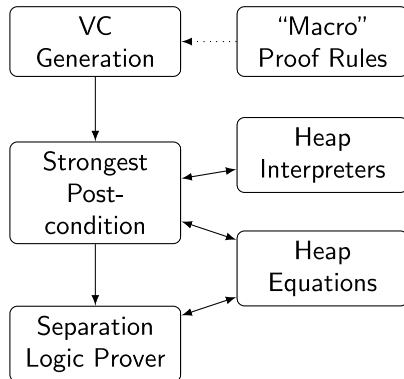

Questions?