



*ParaScope:*  
Advanced Static Analysis for  
*ParaSail,*  
a Parallel Specification and  
Implementation Language

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## Where we are going

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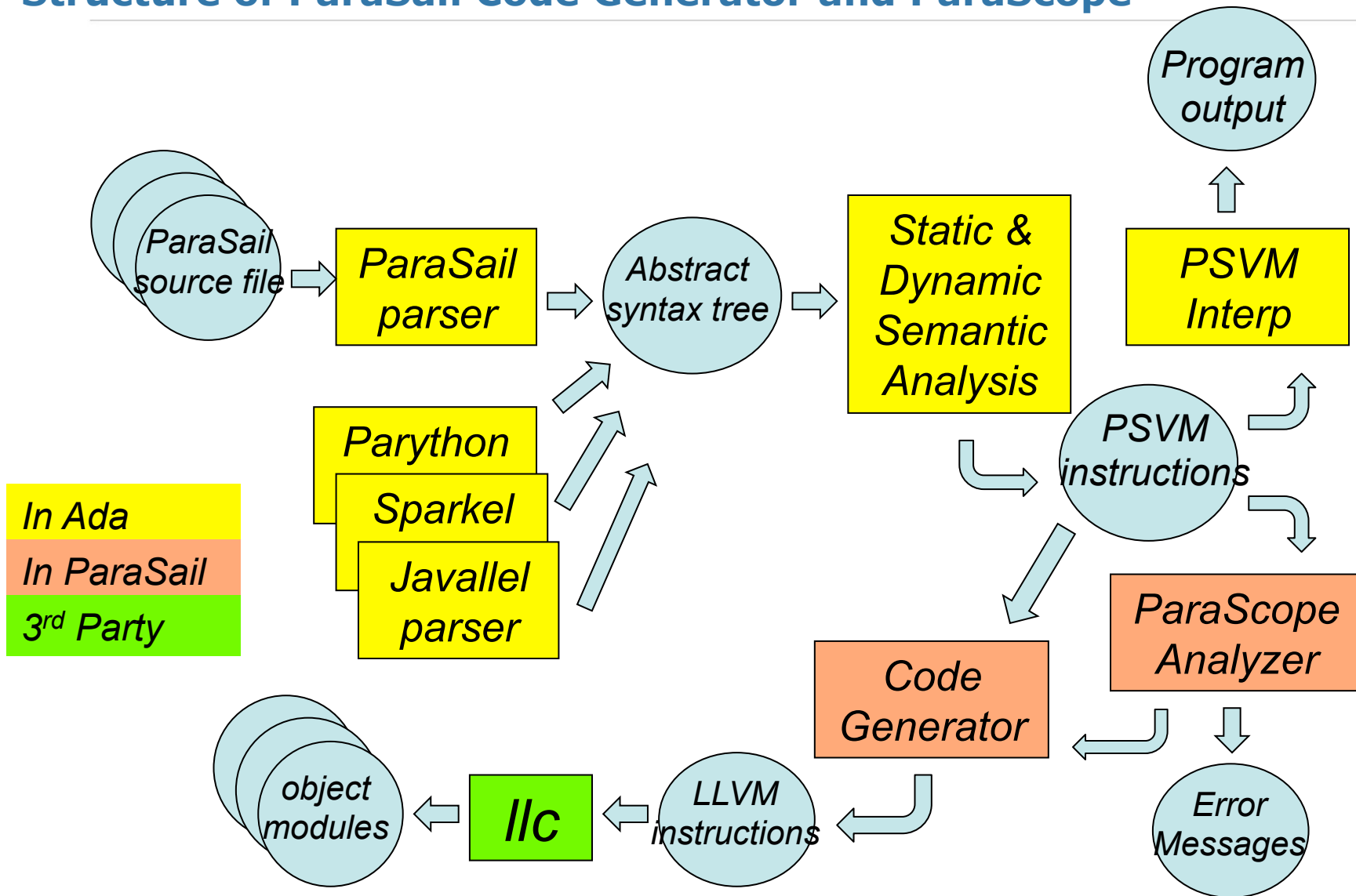
- **Background on ParaSail and ParaScope**
- **Conservative Data Race Detection**
- **Advanced Static Analysis:**
  - Abstract Interpretation and alternatives
- **Value-number approach to Abstract Interpretation in ParaScope Static Analyzer**
- **Inferring pre- and post- conditions in ParaScope**



## ParaSail and ParaScope

- ***ParaSail* – Parallel Specification and Implementation Language**
  - Pervasively Parallel Language, both implicit and explicit
  - Safety through Simplification:
    - No Global Variables
    - No Parameter Aliasing
    - No Re-Assignable Pointers
    - No Unstructured Locking or Signaling
  - Hoare-like syntax for explicit assertion/precondition/postcondition/invariant
  - Conservative Data Race Detection built into ParaSail front end
- ***ParaScope* – ParaSail Static Catcher of Programming Errors**
  - Re-engineered Abstract Interpretation Approach using Value Numbers
  - Integrated into LLVM-Based Code Generator
    - Immediate Feedback to Programmer about all possible Run-Time Errors
      - Identifies possible violations of assertions/preconditions/...
    - Feedback to Code Generator to optimize generated LLVM

## Structure of ParaSail Code Generator and ParaScope



## Conservative Data Race Detection in ParaSail front end

```

class Race_Cond is
  exports
    func Update_Both(var X : Integer;
                    var Y : Integer) is
      X := X + 1 || Y := Y - 1;
    end func Update_Both;
    func Update_One(var X : Integer;
                   Y : Integer) is
      X := X + 10;
    end func Update_One
    func Update_And_Return(var X : Integer)
      -> Integer is
      X := X + 100;
      return X - 50;
    end func Update_And_Return
    func Return_Ref(ref X : Integer)
      -> ref Integer is
      return X;
    end func Return_Ref;
end class Race_Cond;

```

```

Race_Cond::Update_Both(A, B);

Race_Cond::Update_Both(A, A);
** W/W Data Race on A ----- ^ - ^

Race_Cond::Update_One(A, A);
** W/R Data Race on A ----- ^ - ^

Race_Cond::Update_One(A, -A);
A := Race_Cond::Update_And_Return(A);
Race_Cond::Update_One
  (A, Race_Cond::Return_Ref(B));

Race_Cond::Update_One
  (Race_Cond::Return_Ref(A), <--+
   Race_Cond::Return_Ref(A)); |
** W/R Data Race on A -----^ ----- +

Race_Cond::Update_One
  (Race_Cond::Return_Ref(A),
   Race_Cond::Return_Ref(B));

```

## Data Race Detection handles up-level references

```

26  func dummy() is
27      var Up : I1 := create()
28      func B(I : I1);
29      func A() is
30          var X : I1 := create()
31          B(X)
32      end func A
33      func B(I : I1) is
34          read(I)
35          bump(Up)
36      end func B
37      func C() is
38          var Y : I1 := create()
39          B(Y)
40          read(Up)
41      end func C
42      func D() is
43          var Y : I1 := create()
44          B(Y)
45          B(Up) // Data Race with Up
              ^ -- Warning: W/R Data Race on Up
                  at mut_recurse.psl:35:15:
46      end func D
47      A()
48      C()
49      D()
50      block
51          A()
52      ||
53      C() // Data races
              ^ -- Warning: W/W Data Race on Up
                  at mut_recurse.psl:51:9:
              ^ -- Warning: W/R Data Race on Up
                  at mut_recurse.psl:51:9:
54      end block
55      end func dummy

```

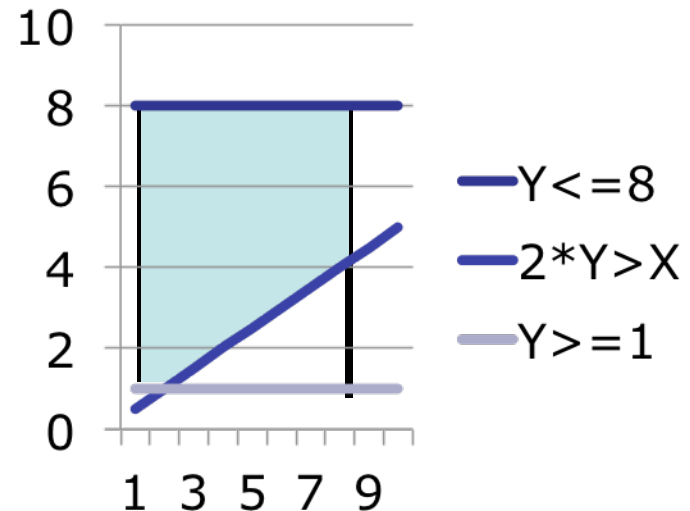
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***ParaScope:***  
**Advanced Static Analysis based on**  
**Re-Engineered Abstract Interpretation**

## What is Abstract Interpretation?

- Approximates the set of possible states of all variables at each point in a program, to allow proofs for safety, security, or correctness.
- Iterates until a fixed-point, then checks for violations.
- *Constructs* the set of possible values, rather than *searching* through them (handles large ranges).
- Represents relationships, e.g.  $2*Y > X$ , using, e.g. polygons/polyhedrons

**X in 1..8, Y in 1..8,  $2*Y > X$ :**





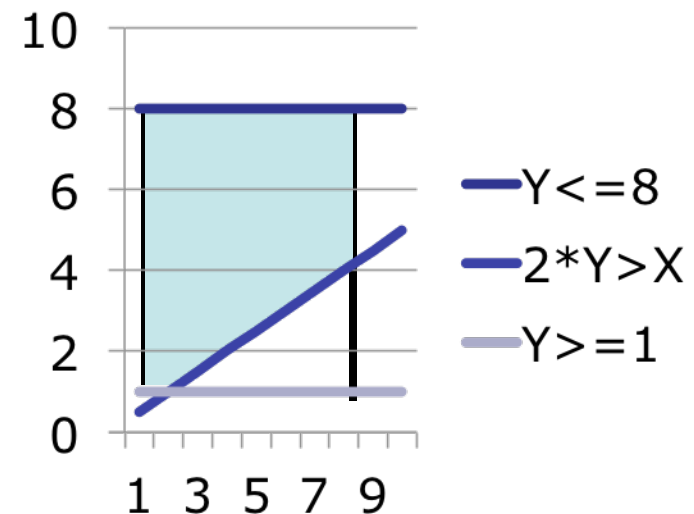
## Alternative Program Proof Techniques

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- **Model Checking (e.g. SPIN model checker)**
  - Searches through state space for states that violate desirable properties
  - State explosion is a challenge; may limit loop iterations
  - Symbolic Model Checking can help
- **Formal Proof (e.g. SPARK 2014 toolset)**
  - Constructs a series of Verification Conditions (VCs) that represent desired safety, security, or correctness properties that should hold at various points in the program
  - Use SMT Solver or equivalent to prove each Verification Condition
  - Use timeout to determine VC cannot be proved
  - Typically relies on programmer to provide pre/postconditions, loop invariants, etc.

## What is the problem with “classic” Abstract Interpretation?

- **Polyhedral representation of relationships between variables is fundamentally limiting (e.g.  $Y > B - X*Z/A$ )**
- **Many approaches exist (courtesy of Wikipedia):**
  - congruence relations on integers
  - convex polyhedra (high computational costs)
  - “octagons”
  - difference-bound matrices
  - linear equalities
- **Other issues:**
  - Initial value set for inputs may require exploring all paths that reach procedure
  - May require a driver or harness to provide realistic input values



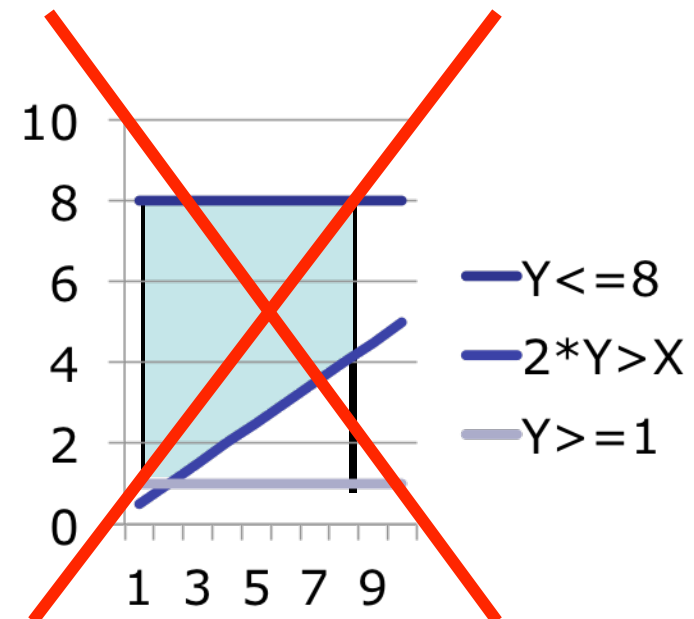
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## Can we Re-Engineer Abstract Interpretation to solve this?

### Basic Trick used in ParaScope Static Analyzer:

- Trick first learned in 1982 from Bob Morgan for Ada compiler
- Use "Value Numbers" to represent value of computing *interesting* expressions (e.g. " $Y * 2 - X$ ")
- Associate Value Sets (Vsets) with Value Numbers (VNs)
- Unlike variables, value numbers don't *change* in value over time
  - *but what we know about them does*
- Value set "*shrinks*" when we do a conditional jump
  - e.g. **if**  $Y * 2 > X$  **then** ...
    - in **then** part we know " $Y * 2 - X$ " in  $1 .. +inf$
    - in **else** part we know " $Y * 2 - X$ " in  $-inf .. 0$
- Also *shrinks* when we do a check or an assertion
  - e.g. **assert**  $X + Y > Z \rightarrow "X + Y - Z"$  in  $1 .. +inf$

## How do Value Numbers simplify value-set determination?

- Only need to represent simple sets of integers, floats, or addresses for each value number (no polyhedrons!)
- Relationships between VNs are represented in value-number definition table (aka *computation table*)
- All variables/expressions with same value share a VN
- Each *basic block* and *edge* of Control Flow Graph (CFG) has its own *map* from VN to Value Set
- When one VN's Vset shrinks, we can efficiently *propagate* it to all related VNs in same map

Typical VN=>Vset Map:

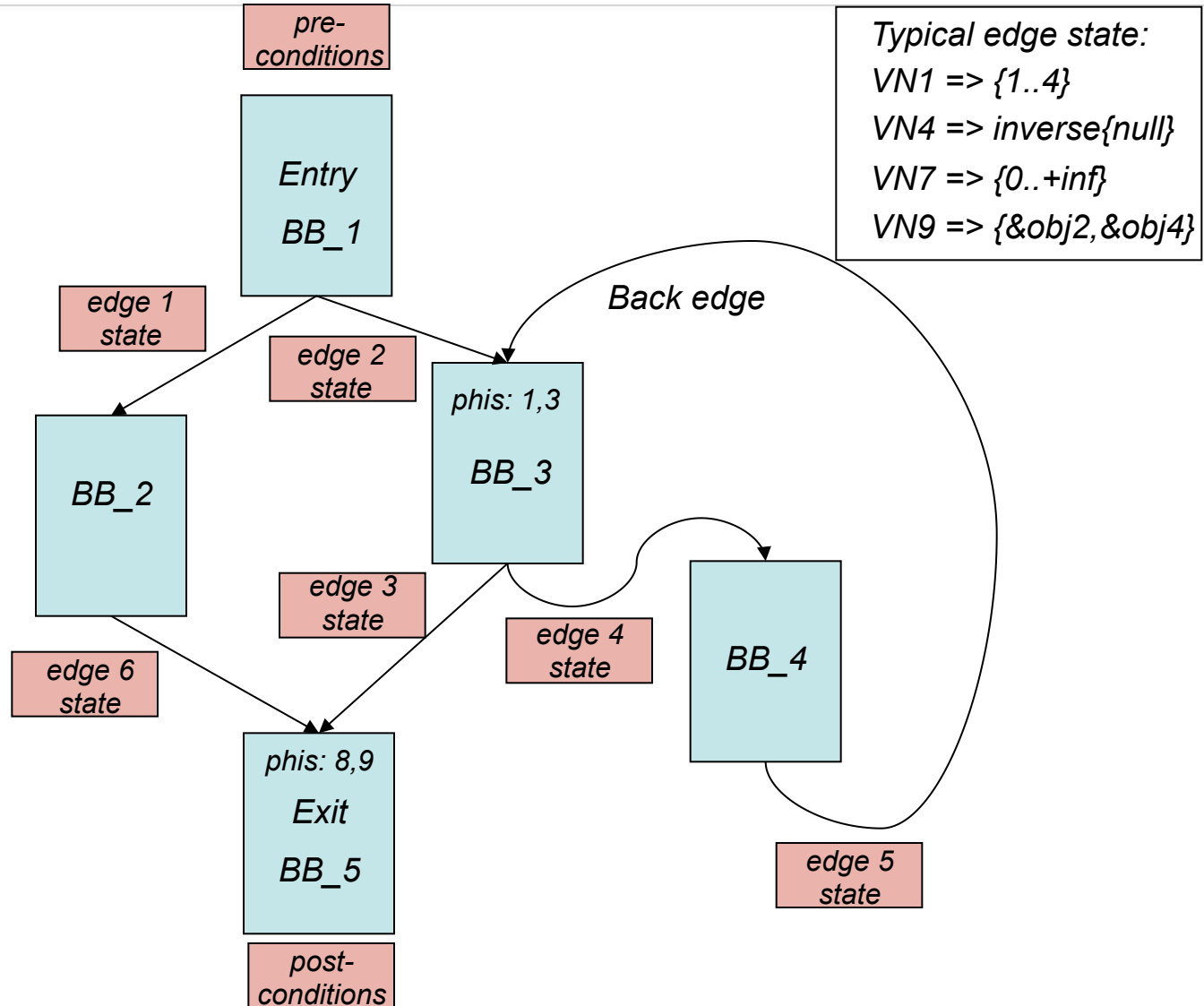
$VN1 \Rightarrow \{1..4\}$

$VN4 \Rightarrow \text{inverse}\{\text{null}\}$

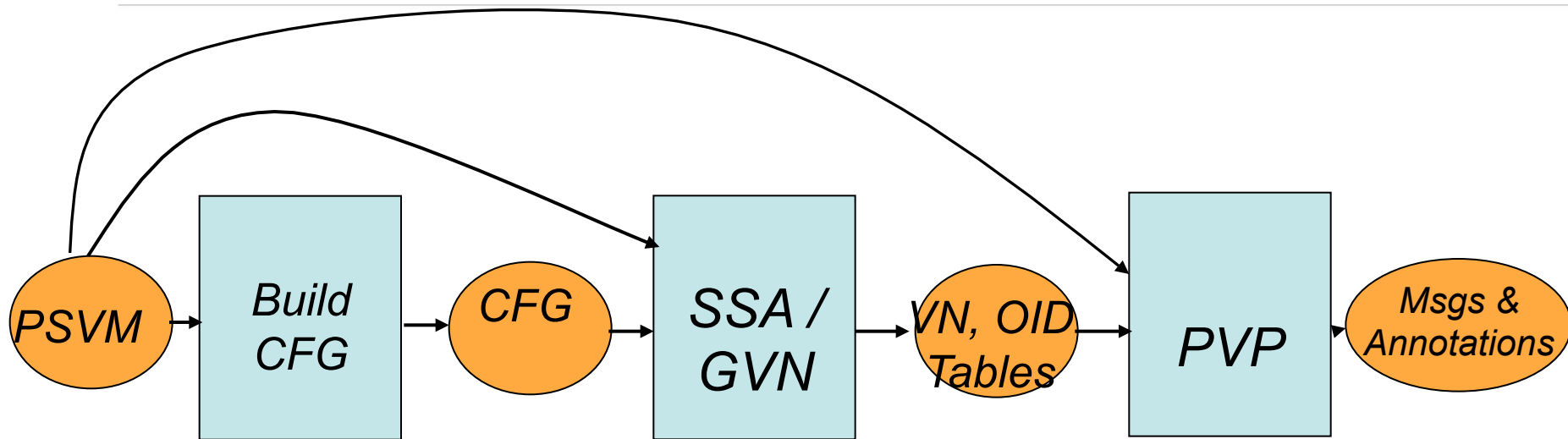
$VN7 \Rightarrow \{0..+\text{inf}\}$

$VN9 \Rightarrow \{\&\text{obj2}, \&\text{obj4}\}$

# Typical Control Flow Graph



## Overall 3-phase Structure of ParaScope Static Analyzer



### *ParaScope Phase Responsibilities*

- CFG* { • *Identifies Basic Blocks and Builds (Sequentialized) CFG*
- SSA* { • *Converts into Single-Static-Assignment form*  
• *Globally Assigns Origin IDs and Value Numbers*
- PVP* { • *Propagates Value Sets and Gives Warnings*

## Static Single Assignment/Global Value Numbering (SSA/GVN) phase

*Dominator  
Tree & Loop  
Identification*

*SSA Phi  
Placement*

*Global Value  
Numbering*

*VN Live  
Ranges*

- *Walk the “Control Flow Graph” of basic blocks and find loops, etc.*
- *Assign a unique “value number” to every fetch of a variable and every computation*
- *Use “phi” value numbers at join points to represent alternative values*
  - *E.g. if  $X > Y$  then  $Max := X$  else  $Max := Y$  end if;  $Max == ? \Rightarrow PhiVN(X, Y)$*
- *“Kappa” node introduced to represent value of potential alias after assignment*
  - *E.g.  $A[I] := 3$ ;  $A[J] := 5$ ;  $A[I] == ? \Rightarrow KappaVN(I == J? 5: 3)$*



## Goals of Possible Value Propagation (PVP) Phase

- **Compute Possible Value Set for every Value Number in every Basic Block**
  - Map of Value number to Value set
- **Check for failures of run-time checks, user assertions, and preconditions of called routines**
  - Initially assume checks will pass and thereby infer Pre/Postconditions
  - Iterate until a fixed point
  - Make final pass to report checks that still fail

*Typical VN=>Vset Map:*  
VN1 => {1..4}  
VN4 => inverse{null}  
VN7 => {0..+inf}  
VN9 => {&obj2, &obj4}

## PVP Iterative Cycle

- **Works one basic-block (BB) at a time.**
- **Initializes the “checks” table for each BB**
  - Summary of all “implicit” and “explicit” checks performed in BB for each VN
- **Applies checks of BB and then propagates changes in VN value sets until they stabilize**
  - Propagate “down” to constituent VNs, then “up” to composite VNs
  - e.g.  $VN1 = VN2 * VN3$ 
    - Shrink VN1, propagate “down” to VN2 and VN3;
    - Shrink VN3, propagate “up” to VN1.
- **Computes VN state for each BB and for each outgoing edge**
  - Saves edge states for later iterations
  - Saves exit-block state for pre/postconditions

## Example of PVP warning messages

```

func Scope_Test
  (X : optional Integer;
   Y : optional Integer) -> Integer is
  var R : Countable_Range<Integer>
      := X .. Y
  **      ^ --- ^ Operands might be null
  R := R.First + 2 .. R.Last + 2
  {R.Last - 2 == Y}
  **      ^ -- Assertion Might Fail §
  var L : List<Integer> :=
      (Elem => 3, Next => null)
  const A := L.Elem
  L.Elem := L.Elem + 5
  const B := L.Elem + A
  L.Next := (Elem => B, Next => null)
  {L.Next.Elem == 11}
  {B == A + 6}
  **      ^ -- Assertion will fail here
  {B > X}
  **      ^ -- Assertion might fail

```

§ False Positive (associativity NYI)

```

if X is null then
  ** Edge 9 is dead; cannot reach here
  return 6
elseif Y is null then
  ** Edge 12 is dead; cannot reach here
  {(X not null) == #true}
  return X
else
  {X is null and Y is null}
  **      ^ -- Assertion will fail here
  if X > Y then
    {X - Y > 0}
    return X - Y
  else
    {X - Y <= 0}
    null
  end if
end if
** Uninitialized function result here
end Scope_Test

```

## Inferring Preconditions in PVP phase

- **Each Input** (parameter or global) is given an “Input VN” to represent its (unknown) *initial* value
- **Vset for Input VN is full possible range of type**
  - **e.g.** Inp\_VN1 in  $-2^{31} .. +2^{31}-1$
- **As we apply checks and assertions Vset for Input VN may shrink, eliminating the “bad” values.**
- **VNs corresponding to combinations of Inputs and Literals** (e.g.  $\text{Inp\_VN1} - \text{Inp\_VN2} * 2$ ) **might also undergo checks/assertions and might shrink** (directly or indirectly)
- **At exit block, Vset of Input VN or combination thereof represents the “good” values** (those that survived the checks and assertions), **i.e. a precondition**

**e.g.**  $\text{Inp1} - \text{Inp2} * 2$  in  $1 .. +\text{inf}$ ;       $\text{Inp2}$  in  $-\text{inf} .. -1 \mid +1 .. +\text{inf}$

→ **Preconditions:**  $\text{Inp1} > \text{Inp2} * 2$ ;       $\text{Inp2} \neq 0$

## Inferring Postconditions in PVP phase

Same principle applies for Postconditions ...

- **In Exit Block, Vset associated with a VN that represents the final value of some Output** (parameter, global, or function result) **or combination thereof, represents possible values upon completion, i.e. a *postcondition***

- ***Example:***

```

proc Incr(X : in out Integer) is
  X := X + 1
end proc Incr

```

*initial value of X is Inp\_VN1:*

*Inp\_VN1 in  $-2^{31} .. +2^{31}-1$*

*final value of X is VN2 = Inp\_VN1 + 1:*

*VN2 in  $-2^{31}+1 .. +2^{31}$*

*check that X + 1 doesn't overflow:*

*VN2 in  $-2^{31}+1 .. +2^{31}-1$*

*propagates to:*

*Inp\_VN1 in  $-2^{31} .. +2^{31}-2$*

→ *precondition:  $X'Initial \leq 2^{31}-2$*

→ *postcondition:  $X'Final$  in  $-2^{31}+1 .. +2^{31}-1$ ;  $X'Final = X'Initial+1$*

## Screen shot showing Inferred Pre/Postconditions

```

P/P  -- Subp: fsw_example
      --
      -- Preconditions:
      --   N >= 1
      --
      -- Postconditions:
      --   A = One-of{1, 101, N - 1}
      --   A in (0..121 | 789..231-2)
      --   B = One-of{2, 102, N}
      --   B in (1..122 | 790..231-1)
      --   B = A + 1
      --
      -- Test Vectors:
      --   N: {123..456}, {457..789}, {1..122 | 790..231-1}
      --   A: {1}, {101}
      --   B: {2}, {102}
      --
2    procedure Fsw_Example (N : Natural;
3                               A, B : out Natural) is
4    begin
5      case N is
6        when 123 .. 456 =>
7          A := 1;
8          B := 2;
9        when 457 .. 789 =>
10         A := 101;
11         B := 102;
12        when others =>
13         A := N - 1;
14         B := N;
15      end case;
16      pragma Assert (B - A = 1);
17    end Fsw_Example;

```

## Summary

- **ParaSail Simplifies Conservative Data Race Detection**
  - Lack of Re-Assignable Pointers and Parameter Aliasing simplify problem
  - Can do checks at compile-time
  - Simplifies later static analysis
- **ParaScope Advanced Static Analysis Integrated with Compiler**
  - Uses Re-Engineered Abstract Interpretation based on Value Numbering
  - Assumes No data races are possible so can treat as sequential program
  - Gives immediate feedback to programmer about all possible run-time errors
- **Re-engineered value-number based approach in ParaScope:**
  - Can represent arbitrary relationships between variables
  - Uses efficient mechanism to propagate information between value numbers
  - Can infer both numeric and symbolic pre/postconditions so no need for drivers/harnesses or top-down walk